# **Lanesfield Primary School**



# **UKS2 Calculation Policy**

The policy provides examples of calculation methods for each year group.

It uses the concrete, pictorial and abstract approach to develop solving.

fluency, reasoning and problem

Review Date: June 2024

### **KEY STAGE 2**

In upper Key Stage 2, children build on secure foundations in calculation, and develop fluency, accuracy and flexibility in their approach to the four operations. They work with whole numbers and adapt their skills to work with decimals, and they continue to develop their ability to select appropriate, accurate and efficient operations.

**Key language:** decimal, column methods, exchange, partition, mental method, ten thousand, hundred thousand, million, factor, multiple, prime number, square number, cube number

Addition and subtraction: Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage.

Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods.

Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen.

**Multiplication and division:** Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers.

Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000.

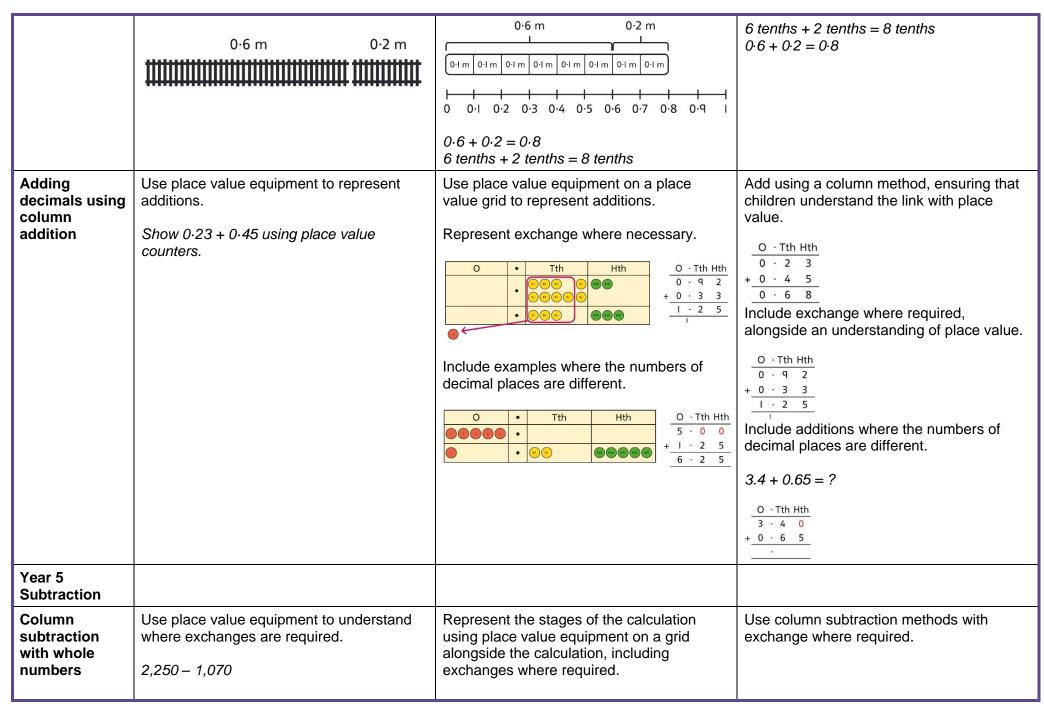
Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions.

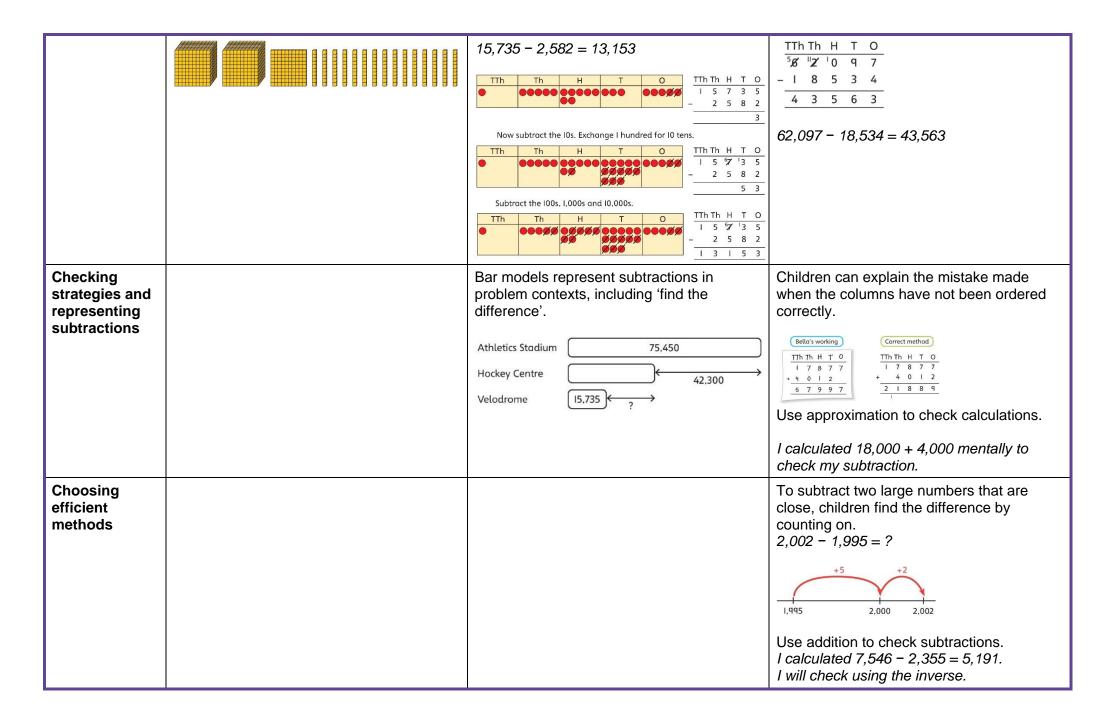
Multiplication and division of decimals are also introduced and refined in Year 6.

Fractions: Children find fractions of amounts, multiply a fraction by a whole number and by another fraction, divide a fraction by a whole number, and add and subtract fractions with different denominators. Children become more confident working with improper fractions and mixed numbers and can calculate with them. Understanding of decimals with up to 3 decimal places is built through place value and as fractions, and children calculate with decimals in the context of measure as well as in pure arithmetic.

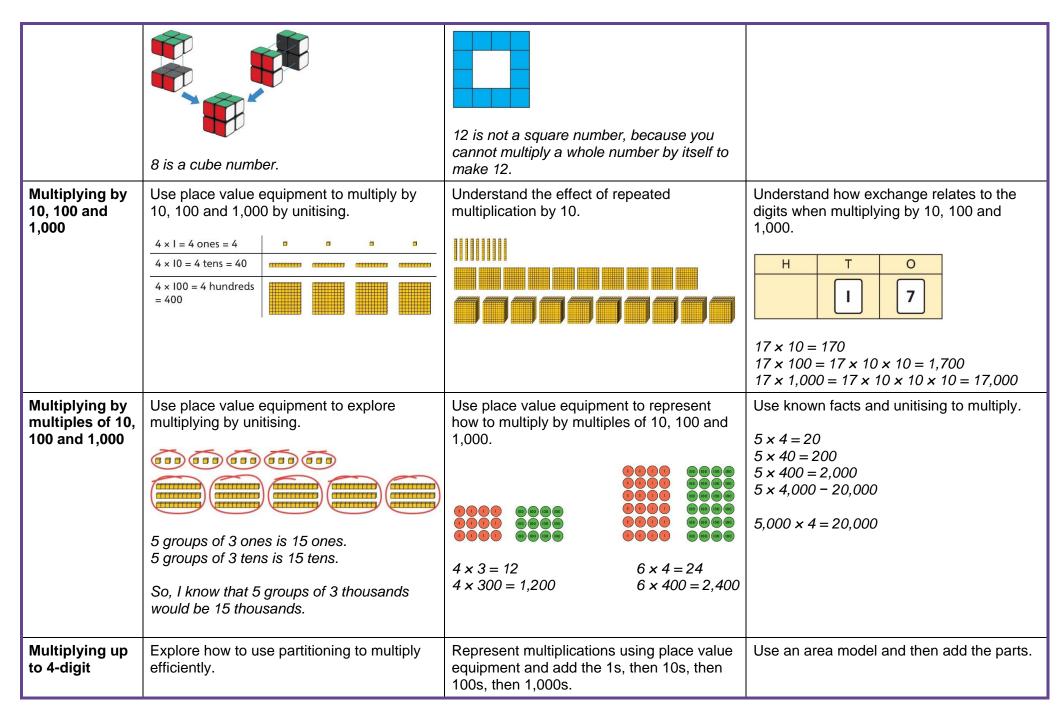
Children develop an understanding of percentages in relation to hundredths, and they understand how to work with common percentages: 50%, 25%, 10% and 1%.

	Year 5			
	Concrete	Pictorial	Abstract	
Year 5 Addition				
Column addition with whole numbers	Use place value equipment to represent additions.  Add a row of counters onto the place value grid to show 15,735 + 4,012.	Represent additions, using place value equipment on a place value grid alongside written methods.   The description of the desc	Use column addition, including exchanges.    TTh Th	
Representing additions		Bar models represent addition of two or more numbers in the context of problem solving.    FIRST	Use approximation to check whether answers are reasonable.    TTh Th H T O   TTh Th H T O   2 3 4 0 5   + 7 8 9 2   + 7 8 9 2   3 1 2 9 7	
Adding tenths	Link measure with addition of decimals.  Two lengths of fencing are 0.6 m and 0.2 m.  How long are they when added together?	Use a bar model with a number line to add tenths.	Understand the link with adding fractions. $\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$	



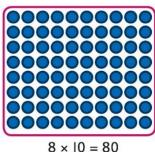


Subtracting decimals	Explore complements to a whole number by working in the context of length. $ \boxed{0.49 \text{ m}} $ $ \boxed{1 \text{ m} - \boxed{\text{m}} = \boxed{\text{m}} } $ $ 1 - 0.49 = ? $	Use a place value grid to represent the stages of column subtraction, including exchanges where required. $5.74 - 2.25 = ?$ O Tth Hth $5.74 - 2.25 = ?$ Exchange I tenth for I0 hundredths.  O Tth Hth $5.67 + 4$ $-2.25$ Now subtract the 5 hundredths.  O Tth Hth $5.67 + 4$ $-2.25$ Now subtract the 5 hundredths.  O Tth Hth $5.67 + 4$ $-2.25$ Now subtract the 2 tenths, then the 2 ones.  O Tth Hth $5.67 + 4$ $-2.25$	Use column subtraction, with an understanding of place value, including subtracting numbers with different numbers of decimal places.  3.921 - 3.75 = ?  O Tth Hth Thth 3 Q Q I - 3 7 5 0 - 3 7 5 0
Year 5 Multiplication			
Understanding factors	Use cubes or counters to explore the meaning of 'square numbers'.  25 is a square number because it is made from 5 rows of 5.  Use cubes to explore cube numbers.	Use images to explore examples and non-examples of square numbers.  8 × 8 = 64 8 <sup>2</sup> = 64	Understand the pattern of square numbers in the multiplication tables.  Use a multiplication grid to circle each square number. Can children spot a pattern?



# numbers by a single digit

$$8 \times 17 = ?$$



000000
000000
8 × 7 = 56

Н	Т	0
(00)	000000	000
<b>(00)</b>	00000	000
000	10 10 10 10	000
(iii)	000000	000
<u></u>	000000	000

	100	60	3
5	$100 \times 5 = 500$	60 × 5 = 300	3 × 5 = 15

Use a column multiplication, including any required exchanges.

## **Multiplying 2**digit numbers by 2-digit numbers

Partition one number into 10s and 1s, then add the parts.

$$23 \times 15 = ?$$

80 + 56 = 136

So,  $8 \times 17 = 136$ 







н т о

1 5 0

1 5 0

3 4 5

+ 4 5



There are 345 bottles of milk in total.

$$23 \times 15 = 345$$

Use an area model and add the parts.

$$28 \times 15 = ?$$

	20 m	8 m	
10 m	20 × 10 = 200 m <sup>2</sup>	8 × I0 = 80 m <sup>2</sup>	
5 m	20 × 5 = 100 m <sup>2</sup>	$8 \times 5 = 40 \text{ m}^2$	+

$$28 \times 15 = 420$$

Use column multiplication, ensuring understanding of place value at each stage.

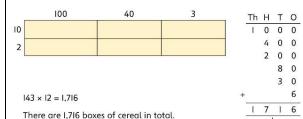
2 0 0

1 0 0 8 0

4 2 0

# Multiplying up to 4-digits by 2-digits

Use the area model then add the parts.



$$143 \times 12 = 1,716$$

Use column multiplication, ensuring understanding of place value at each stage.

Progress to include examples that require multiple exchanges as understanding, confidence and fluency build.

 $1.274 \times 32 = ?$ First multiply 1,274 by 2.

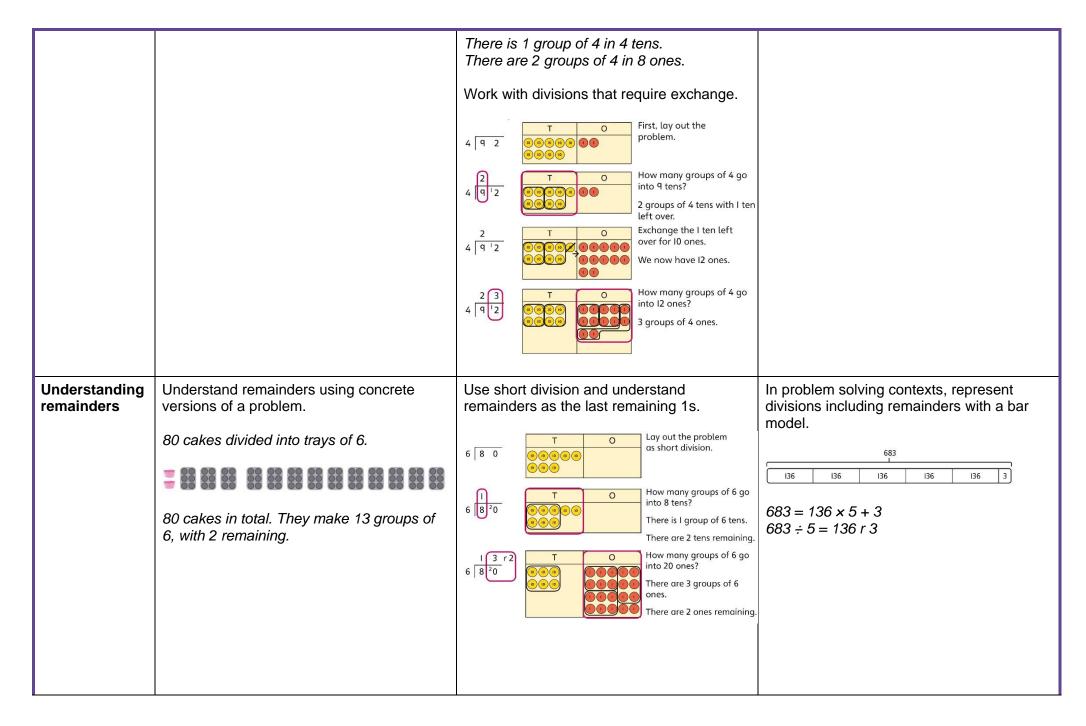
Then multiply 1,274 by 30.

Finally, find the total.

Multiplying decimals by 10, 100 and 1,000	Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.	Represent multiplication by 10 as exchange on a place value grid.  O Tth Hth O O O O O O O O O O O O O O O O O O O	Understand how this exchange is represented on a place value chart. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Year 5 Division			
Understanding factors and prime numbers	Use equipment to explore the factors of a given number.  24 ÷ 3 = 8 24 ÷ 8 = 3 8 and 3 are factors of 24 because they divide 24 exactly.  24 ÷ 5 = 4 remainder 4.  5 is not a factor of 24 because there is a remainder.	Understand that prime numbers are numbers with exactly two factors. $13 \div 1 = 13$ $13 \div 2 = 6 r 1$ $13 \div 4 = 4 r 1$ 1 and 13 are the only factors of 13. 13 is a prime number.	Understand how to recognise prime and composite numbers.  I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder.  I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33.  I know that 1 is not a prime number, as it has only 1 factor.
Understanding inverse operations and the link with multiplication, grouping and sharing	Use equipment to group and share and to explore the calculations that are present.  I have 28 counters.  I made 7 groups of 4. There are 28 in total.	Represent multiplicative relationships and explore the families of division facts.	Represent the different multiplicative relationships to solve problems requiring inverse operations.

	I have 28 in total. I shared them equally into 7 groups. There are 4 in each group.  I have 28 in total. I made groups of 4. There are 7 equal groups.	60 ÷ 4 = 15 60 ÷ 15 = 4	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Dividing whole numbers by 10, 100 and 1,000	Use place value equipment to support unitising for division. $4,000 \div 1,000$ $4,000 \times 1,000 \times 1,000$	Use a bar model to support dividing by unitising. $380 \div 10 = 38$ 380  7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.  The Head Toology The Toolo
Dividing by multiples of 10, 100 and 1,000	Use place value equipment to represent known facts and unitising.	Represent related facts with place value equipment when dividing by unitising.	Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check. $3,000 \div 5 = 600$ $3,000 \div 50 = 60$ $3,000 \div 500 = 6$ $5 \times 600 = 3,000$

	15 ones put into groups of 3 ones. There are 5 groups. 15 ÷ 3 = 5  15 tens put into groups of 3 tens. There are 5 groups.  150 ÷ 30 = 5	180 is 18 tens.  18 tens divided into groups of 3 tens. There are 6 groups.  180 $\div$ 30 = 6  1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$50 \times 60 = 3,000$ $500 \times 6 = 3,000$
Dividing up to four digits by a single digit using short division	Explore grouping using place value equipment. $268 \div 2 = ?$ There is 1 group of 2 hundreds. There are 3 groups of 2 tens. There are 4 groups of 2 ones. $264 \div 2 = 134$	Use place value equipment on a place value grid alongside short division. The model uses grouping. A sharing model can also be used, although the model would need adapting.  The model would need adapting.  The model would need adapting.  The model would need adapting.	Use short division for up to 4-digit numbers divided by a single digit. $ \begin{array}{cccccccccccccccccccccccccccccccccc$



Understanding the relationship between fractions and division.  1 whole shared between 3 people. Each person receives one-third.  1 $\div$ 3 = $\frac{1}{3}$ Use a bar model and other fraction representations to show the link between fractions and division.  1 whole shared between 3 people. Each person receives one-third.  1 $\div$ 3 = $\frac{1}{3}$ 1 $\div$ 4 = $\frac{11}{4}$ = $2\frac{3}{4}$ Year 6	Dividing decimals by 10, 100 and 1,000	Understand division by 10 using exchange.  2 ones are 20 tenths.  20 tenths divided by 10 is 2 tenths.	Represent division using exchange on a place value grid.  O Tth Hth  O Tth Ht	Understand the movement of digits on a place value grid.  O Tth Hth Thth O 8 5 O 90
	the relationship	fractions and division.  1 whole shared between 3 people. Each person receives one-third.	Use a bar model and other fraction representations to show the link between fractions and division.  I $\div$ 3 = $\frac{1}{3}$	to calculate divisions. $5 \div 4 = \frac{5}{4} = 1\frac{1}{4}$
Concrete   Pictorial   Abstract		Concrete	Pictorial	Abstract

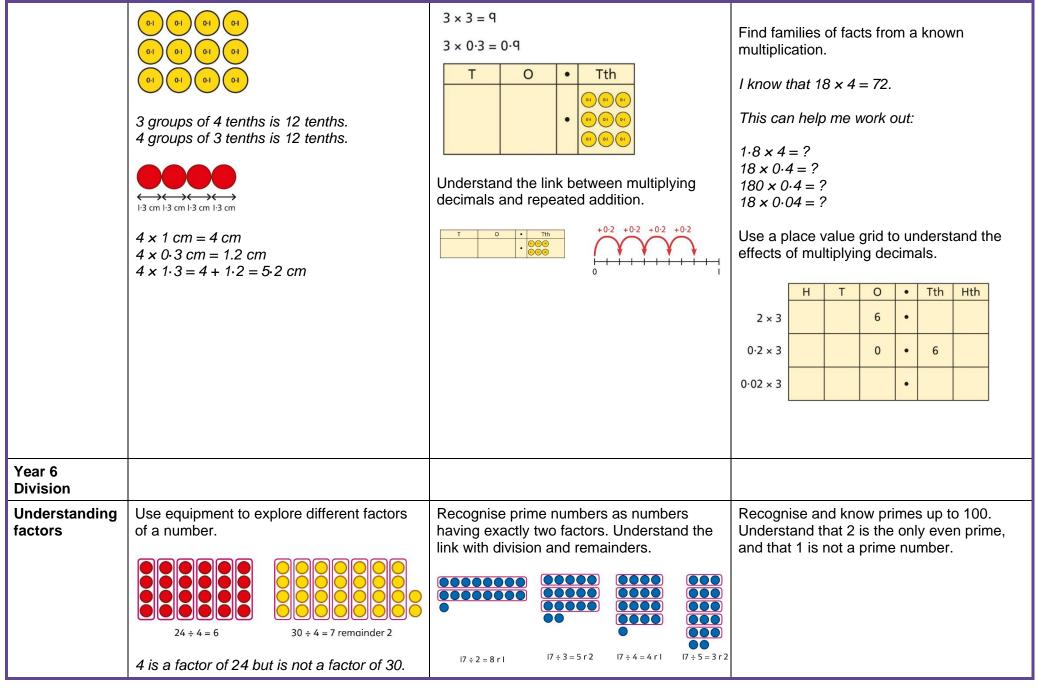
### Year 6 Addition Comparing Represent 7-digit numbers on a place value Discuss similarities and differences Use column addition where mental methods and selecting grid, and use this to support thinking and between methods, and choose efficient are not efficient. Recognise common errors efficient mental methods. methods based on the specific calculation. with column addition. Compare written and mental methods methods HTh TTh Th alongside place value representations. 32,145 + 4,302 = ?0000 TTh Th H T O TTh Th H T O 3 2 1 4 5 40,265 43,265 + 4 3 0 2 + 4 3 0 2 7 5 1 6 5 3 6 4 4 7 TTh 0 4 0 2 6 5 0000 3 5 2 2 Which method has been completed 0000000 accurately? Use bar model and number line What mistake has been made? representations to model addition in problem-solving and measure contexts. Column methods are also used for decimal additions where mental methods are not +I hour efficient. +8 minutes T O · Tth Hth 12:05 13:05 13:13 189.98 Represent 7-digit numbers on a place value Use place value and unitising to support Selecting Use a bar model to support thinking in grid, and use this to support thinking and mental calculations with larger numbers. mental addition problems. methods for mental methods. larger numbers 257,000 + 99,000 = ?195,000 + 6,000 = ?where M HTh TTh Th H appropriate 195 + 5 + 1 = 201£257,000 £100,000 2,411,301 + 500,000 = ?195 thousands + 6 thousands = 201thousands

	This would be 5 more counters in the HTh place.  So, the total is 2,911,301.  2,411,301 + 500,000 = 2,911,301	I added 100 thousands then subtracted 1 thousand.  257 thousands + 100 thousands = 357 thousands  257,000 + 100,000 = 357,000  357,000 - 1,000 = 356,000  So, 257,000 + 99,000 = 356,000	So, 195,000 + 6,000 = 201,000
Understanding order of operations in calculations	Use equipment to model different interpretations of a calculation with more than one operation. Explore different results. $3 \times 5 - 2 = ?$	Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	Understand the correct order of operations in calculations without brackets.  Understand how brackets affect the order of operations in a calculation. $4 + 6 \times 16$ $4 + 96 = 100$ $(4 + 6) \times 16$ $10 \times 16 = 160$
Year 6 Subtraction			
Comparing and selecting efficient methods	Use counters on a place value grid to represent subtractions of larger numbers.	Compare subtraction methods alongside place value representations.  The Head To O	Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy.  The Heat To Column 1 is 1 i

		Th H T O 2 6 7 9 - 5 3 4 2 1 4 5  Use a bar model to represent calculations, including 'find the difference' with two bars as comparison.  computer game puzzle book f12·50	Use column subtraction for decimal problems, including in the context of measure.  H T O · Tth Hth 3 0 9 · 6 0 - 2 0 6 · 4 0 1 0 3 · 2 0
Subtracting mentally with larger numbers		Use a bar model to show how unitising can support mental calculations.  950,000 - 150,000  That is 950 thousands - 150 thousands  950  950  So, the difference is 800 thousands. 950,000 - 150,000 = 800,000	Subtract efficiently from powers of 10. $10,000 - 500 = ?$
Year 6 Multiplication			
Multiplying up to a 4-digit number by a single digit number	Use equipment to explore multiplications.  Th T O O O O O O O O O O O O O O O O O O	Use place value equipment to compare methods.  Method I  3 2 2 5 3 2 2 5 3 2 2 5 3 2 2 5 1 2 9 0 0	Understand area model and short multiplication.  Compare and select appropriate methods for specific multiplications.

	0.045 4	Method 2	Method 3
	2,345 × 4	Wethod 2	3,000 200 20 5 4 12,000 800 80 20 12,000 + 800 + 80 + 20 = 12,900  Method 4  3 2 2 5  × 4  1 2 9 0 0
Multiplying up to a 4-digit number by a 2-digit number		Use an area model alongside written multiplication.  Method I  1,000 200 30 5 20 20,000 4,000 600 100 1 1,000 200 30 5  × 2 1  5 1×5 3 0 1×30 2 0 0 1×200 1 0 0 0 1×1,000 1 0 0 0 20×5 6 0 0 20×5 6 0 0 20×30 4 0 0 0 20×200 2 5 9 3 5 21×1,235	Use compact column multiplication with understanding of place value at all stages.    1 2 3 5
Using knowledge of factors and partitions to compare methods for multiplications	Use equipment to understand square numbers and cube numbers. $5 \times 5 = 5^2 = 25$ $5 \times 5 \times 5 = 5^3 = 25 \times 5 = 125$	Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.	Use a known fact to generate families of related facts.    170 × II

		5,200 20 5,200 × 20 5,200 × 25 5,200 × 25 5,000 × 20 5,000 × 20 5,000 × 20 5,000 × 20 5,200 × 5 5,200	Use factors to calculate efficiently.  15 $\times$ 16 = $3 \times 5 \times 2 \times 8$ = $3 \times 8 \times 2 \times 5$ = $24 \times 10$ = $240$
Multiplying by 10, 100 and 1,000	Use place value equipment to explore exchange in decimal multiplication.  To the place value equipment to explore exchange in decimal multiplication.  To the place value equipment to explore exchange in decimal multiplication.  To the place value equipment to explore exchange in decimal multiplication.  Exchange each group of ten tenths.  O-3 × 10 = ?  O-3 is 3 tenths.  10 × 3 tenths are 30 tenths.  30 tenths are equivalent to 3 ones.	Understand how the exchange affects decimal numbers on a place value grid. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000. $8 \times 100 = 800$ $8 \times 300 = 800 \times 3$ $= 2,400$ $2.5 \times 10 = 25$ $2.5 \times 20 = 2.5 \times 10 \times 2$ $= 50$
Multiplying decimals	Explore decimal multiplications using place value equipment and in the context of measures.	Represent calculations on a place value grid.	Use known facts to multiply decimals. $4 \times 3 = 12$ $4 \times 0.3 = 1.2$ $4 \times 0.03 = 0.12$ $20 \times 5 = 100$ $20 \times 0.5 = 10$ $20 \times 0.05 = 1$



			I       2       3       4       5       6       7       8       9       10         II       12       13       14       15       16       17       18       19       20         21       22       23       24       25       26       27       28       29       30         31       32       33       34       35       36       37       38       39       40         41       42       43       44       45       46       47       48       49       50
Dividing by a single digit	There are 78 in total. There are 6 groups of 13. There are 13 groups of 6.	H T O How many groups of 6 are in 100?  How many groups of 6 are in 13 tens?  H T O How many groups of 6 are in 13 tens?  How many groups of 6 are in 12 ones?  How many groups of 6 are in 12 ones?	Use short division to divide by a single digit. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Dividing by a 2-digit number using factors	Understand that division by factors can be used when dividing by a number that is not prime.	Use factors and repeated division. $1,260 \div 14 = ?$ $1,260 \div 2 = 630$ $1,260 \div 7 = 90$	Use factors and repeated division where appropriate. $2,100 \div 12 = ?$ $2,100 \rightarrow                                  $

		1,260 ÷ 14 = 90	
Dividing by a 2-digit number using long division	Use equipment to build numbers from groups.  182 divided into groups of 13. There are 14 groups.	Use an area model alongside written division to model the process. $377 \div 13 = ?$ $?$ $?$ $?$ $?$ $?$ $?$ $?$ $?$ $?$	Use long division where factors are not useful (for example, when dividing by a 2-digit prime number). Write the required multiples to support the division process. $377 \div 13 = ?$ $\begin{array}{c ccccccccccccccccccccccccccccccccccc$

			Divisions with a remainder explored in problem-solving contexts.
Dividing by 10, 100 and 1,000	Use place value equipment to explore division as exchange.   O The Hth Thth  Divide 20 counters by 10.  O-2 is 2 tenths. 2 tenths is equivalent to 20 hundredths. 20 hundredths divided by 10 is 2 hundredths.	Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Use knowledge of factors to divide by multiples of 10, 100 and 1,000. $40 \div 50 = \bigcirc$ $40 \longrightarrow \div 10 \longrightarrow \div 5 \longrightarrow ?$ $40 \longrightarrow \div 5 \longrightarrow \div 10 \longrightarrow ?$ $40 \div 5 = 8$ $8 \div 10 = 0.8$ So, $40 \div 50 = 0.8$
Dividing decimals	Use place value equipment to explore division of decimals.	Use a bar model to represent divisions. $ \begin{array}{c cccc} 0.8 \\ ? & ? & ? \end{array} $ $ 4 \times 2 = 8 & 8 \div 4 = 2 \\ So, 4 \times 0.2 = 0.8 & 0.8 \div 4 = 0.2 $	Use short division to divide decimals with up to 2 decimal places.  8 $\boxed{4 \cdot 2  4}$ 0 \cdot 8 $\boxed{4 \cdot ^42  4}$ 0 \cdot 5  8 $\boxed{4 \cdot ^42  ^24}$ 0 \cdot 5  3   4  ^42  ^24